



## Antimatter: Storage and Applications

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# Antimatter: Storage and Applications

### ***Abstract:***

Antimatter is a fascinating and elusive substance that has intrigued scientists for nearly a century. It is the opposite of ordinary matter, with opposite electric charges, and is created in high-energy collisions. Despite its potential as an energy source and its applications in many fields, containing antimatter is a significant challenge due to its tendency to annihilate upon contact with normal matter. In this paper, we explore various methods for containing antimatter, including the Penning-Malmberg, cusp, and Paul traps. We also examine the exciting developments in antimatter research, including the ALPHA and BASE experiments at CERN, which aim to study the properties of antimatter. Additionally, we discuss the matter-antimatter asymmetry problem, which remains a central puzzle in physics and explore its potential explanations, such as the anti universe theory. Understanding how to effectively contain antimatter could revolutionize numerous fields, such as energy production, space exploration, and medical treatments, making it an area of ongoing interest and research.

## ***Introduction***

Antimatter, the mirror image of ordinary matter with the same mass but opposite electrical charge, has captivated scientists and science fiction writers alike for decades. While it was first predicted by Paul Dirac in 1928, it wasn't until 1932 that the first positron, the antiparticle of the electron, was discovered in cosmic rays by Carl Anderson. Since then, many other antiparticles have been observed, and the properties of antimatter have been studied extensively in high-energy physics experiments. However, despite its promise as a potential source of energy and a tool for medical imaging, the creation and storage of antimatter remain significant challenges due to its extreme rarity and the difficulty of containing it.

In this paper, we will explore three main topics related to antimatter. First, we will discuss the challenges associated with creating and storing antimatter, including some of the traps used to confine it. Second, we will examine the potential applications of antimatter in various fields, including scientific research, medical imaging, and energy generation. Finally, we will delve into one of the most significant puzzles in modern physics: the matter-antimatter asymmetry problem. We will explore the current state of research in this area and examine some of the potential explanations for this phenomenon.

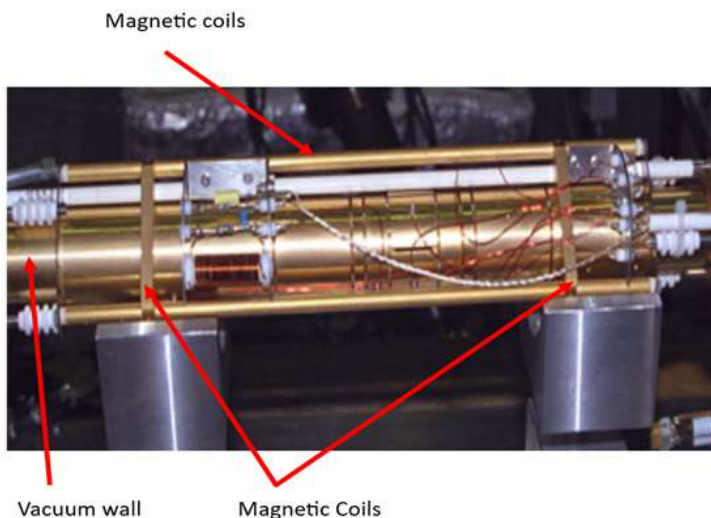
By examining these topics, we hope to provide a comprehensive overview of antimatter and its role in modern physics. Despite the many challenges associated with this enigmatic substance, its potential applications and fundamental mysteries continue to fascinate scientists and inspire ongoing research.

This research paper on antimatter is intended for readers with a basic understanding of physics, including high school students. We will explore the creation and storage challenges, potential applications, and the intriguing matter-antimatter asymmetry problem. Join us on this enlightening journey into the enigmatic realm of antimatter.

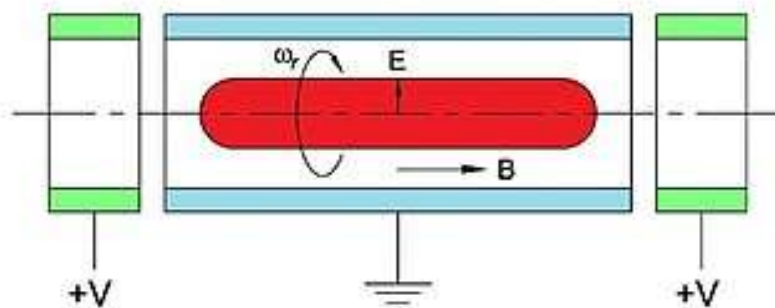
## I. The different confinement methods:

### Penning-Malmberg Trap:

The Penning-Malmberg trap ( Fig 1 & Fig 2) is a type of Penning trap that was invented in the 1980s by Eric A. Malmberg and Stuart J. Penning. It is used to capture and study antimatter particles, such as antiprotons or positrons. The Penning trap for antimatter works by using a combination of magnetic and electric fields to trap the charged particles in a small volume of space. The magnetic field is typically provided by a set of superconducting coils, while the electric field is generated by applying a voltage to a set of electrodes located around the trap.

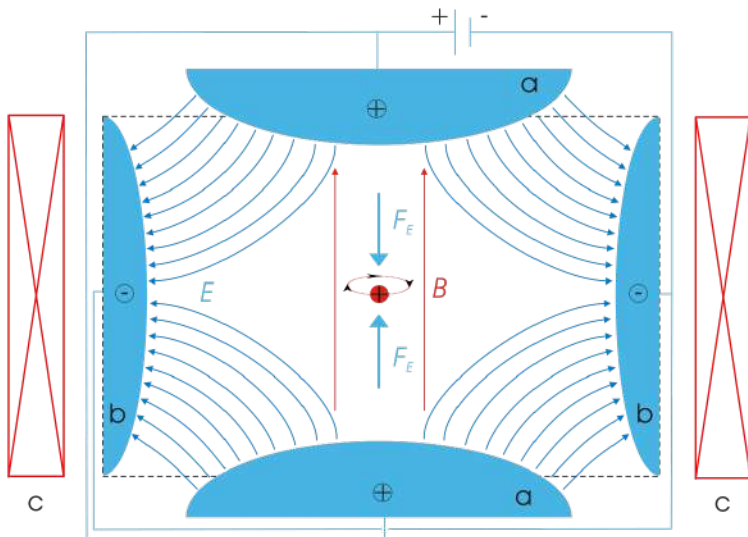


**Figure 1:** This photo shows a Penning trap that uses magnetic and electric fields to hold antimatter in place. The red arrows point to the important parts of the trap.

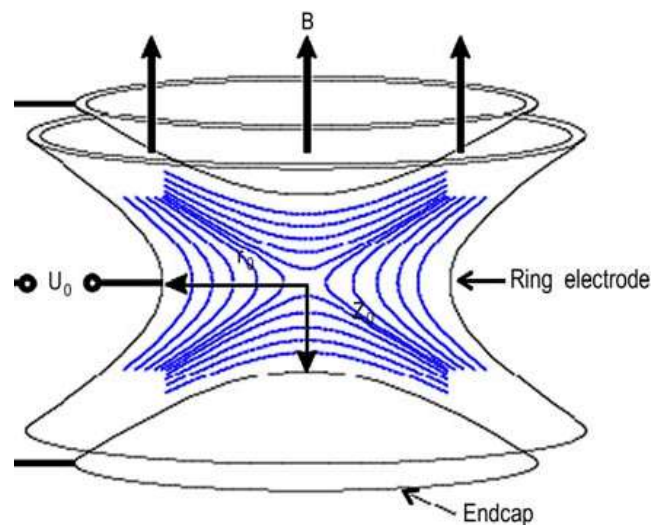


**Figure 2:** Schematic diagram of a Penning–Malmberg trap biased to confine positively charged particles in a set of three cylindrical metal electrodes (green and blue). Due to the particles' charge, there is a radial electric field which causes the plasma to rotate about the magnetic field direction with angular velocity  $\omega_r$ .

In the Penning-Malmberg trap, the magnetic field is produced by a set of cylindrical coils (Fig 2) arranged around the central cylindrical electrode. The electric fields are created by two end cap electrodes and a ring electrode (Fig 4) placed between the endcaps. As shown in figure 4, the ring electrode produces an electric field that cancels out the radial electric field produced by the end caps.



**Figure 4**



**Figure 3**

In **figure 3**, the combination of the magnetic field  $\mathbf{B}$  and electric field  $\mathbf{E}$  creates a potential well that confines the charged particles in all three dimensions. The quadrupole magnetic field also helps to stabilize the motion of the particles, allowing them to remain confined for longer periods of time.

One of the key challenges in building a Penning trap for antimatter is the need to minimize interactions between the trapped particles and the surrounding matter. Any collisions between the antimatter and the trap walls or residual gas molecules could lead to annihilation and the destruction of the antimatter particles.

To mitigate this problem, Penning traps for antimatter are typically operated at extremely low pressures to minimize the number of residual gas molecules in the trap. The trap walls are also typically coated with a thin layer of material, such as gold or graphene, to minimize the chance of collisions.

In recent years, Penning traps for antimatter have been used to perform some of the most precise measurements ever made, with relative uncertainties on the order of  $10^{-10}$  or better. These measurements are opening up new frontiers in our understanding of the fundamental properties of antimatter and are paving the way for future discoveries in this exciting field of research. We will discuss some of these in section 2 .



### ***The limitations of the Penning-Malmberg trap:***

Like any experimental apparatus, the Penning-Malmberg trap has its limitations and drawbacks. Here are a few of them:

1- Charge density limit (Brillouin limit): The trap has a maximum limit on the number of charged particles that can be stored, which is determined by the charge density of the particles.

$$n_B = \frac{\epsilon_0 |\vec{B}|^2}{2m}$$

where B is the magnetic field in the trap, m is the mass of the plasma particles,  $\epsilon_0$  is the permittivity of free space.

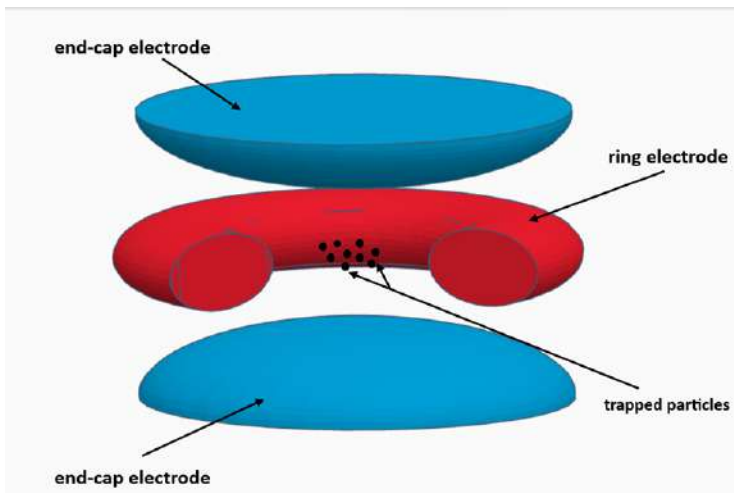
If the charge density becomes too high, the particles can become unstable and escape from the trap.

2- Heating and loss of particles: The oscillating electric field generated by the radio frequency voltage source can cause heating of the particles, leading to their loss from the trap. Additionally, the magnetic field can also cause loss of particles through collisions with the electrodes or other particles.

Despite these limitations, the Penning-Malmberg trap remains an important tool for studying the properties of charged particles, including antimatter. With ongoing developments in technology and experimental techniques, it is likely that the capabilities of the Penning-Malmberg trap will continue to expand, enabling new insights into the fundamental nature of matter and antimatter.

## Paul Trap

The Paul trap is a device that uses alternation between electric fields to trap charged particles, including antimatter particles. It was first proposed by Wolfgang Paul in 1950 and has since become a staple of experimental physics, chemistry, and engineering. The trap consists of a series of electrodes (Fig 5) connected to an alternating current (AC) power supply.

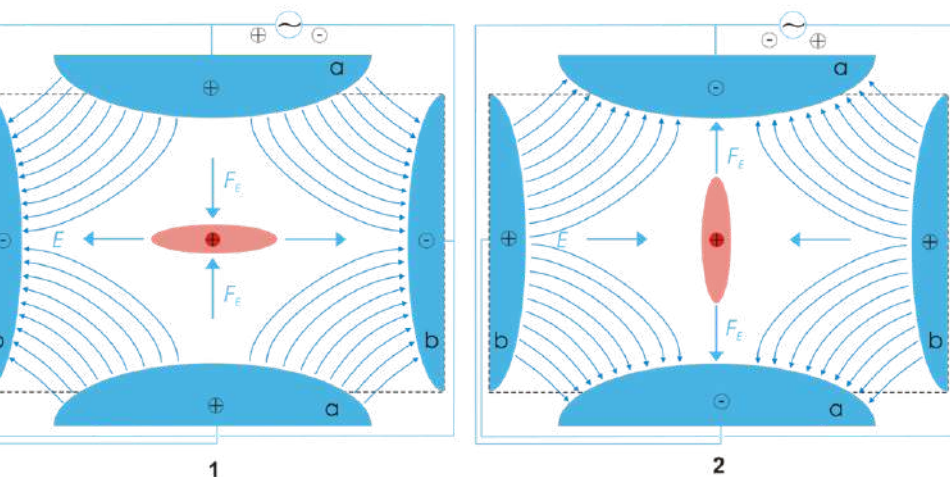


**Figure 5:**

This figure shows the main components of the Paul trap, note that the electrodes are connected to an alternative current (not shown in this figure).

### The Inner Workings of a Paul Trap

As shown in figure 6, the trap operates by using a combination of static  $E$  and radio frequency (RF) electric fields  $F_E$  to confine charged particles within the trap. When a charged particle enters the trap, it experiences a force that depends on its charge and mass, as well as the strength and frequency of the fields. By carefully tuning these parameters, scientists can confine the particle to a small region of space and prevent it from escaping.



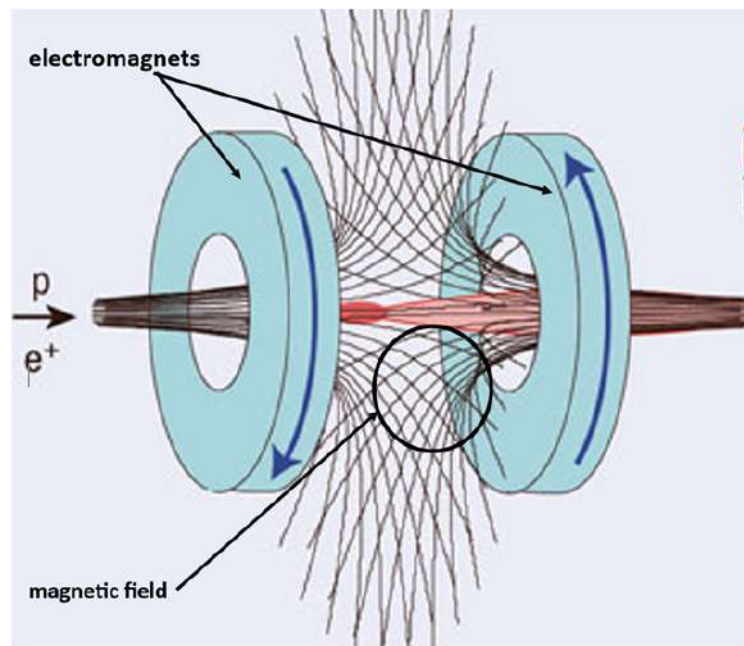
**Figure 6:** Scheme of a Quadrupole ion trap of classical setup with a particle of positive charge (dark red), surrounded by a cloud of similarly charged particles (light red). The electric field  $E$  (blue) is generated by the end-caps (a, positive) and a ring electrode (b). Picture 1 and 2 show two states during an AC cycle.



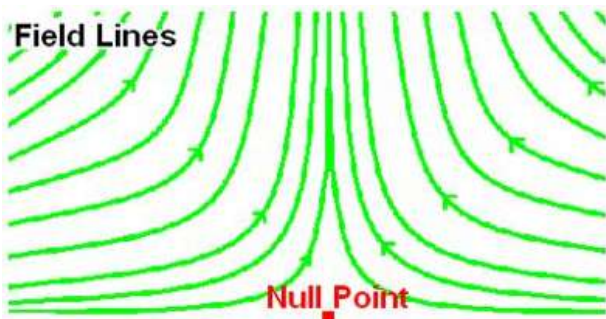
## Cusp trap

A cusp trap is a type of magnetic confinement device that uses a magnetic field (Fig 7) to trap charged particles. The trap gets its name from the shape of the magnetic field, which has a "cusp" or saddle point at the center of the trap. It consists of two parallel electromagnets (Fig 7) with the current running in opposite directions, creating oppositely directed magnetic fields. The two fields interact to form a "null area" (Fig 8) between them where the particles can be trapped.

**Figure 7:** This figure depicts a cusp trap. The black arrows represent the electromagnets that create the magnetic field, while the curved lines illustrate the shape and direction of the field. The cusp trap is designed to confine particles in a specific area using the magnetic field produced by these magnets.



### Geometry of the trap:



**Figure 8:** This figure illustrates the magnetic field lines and null point of a cusp trap. The curved lines represent the magnetic field lines created by the electromagnets in the trap. The null point, which is the point where the magnetic field strength is zero, is shown at the bottom of the figure.

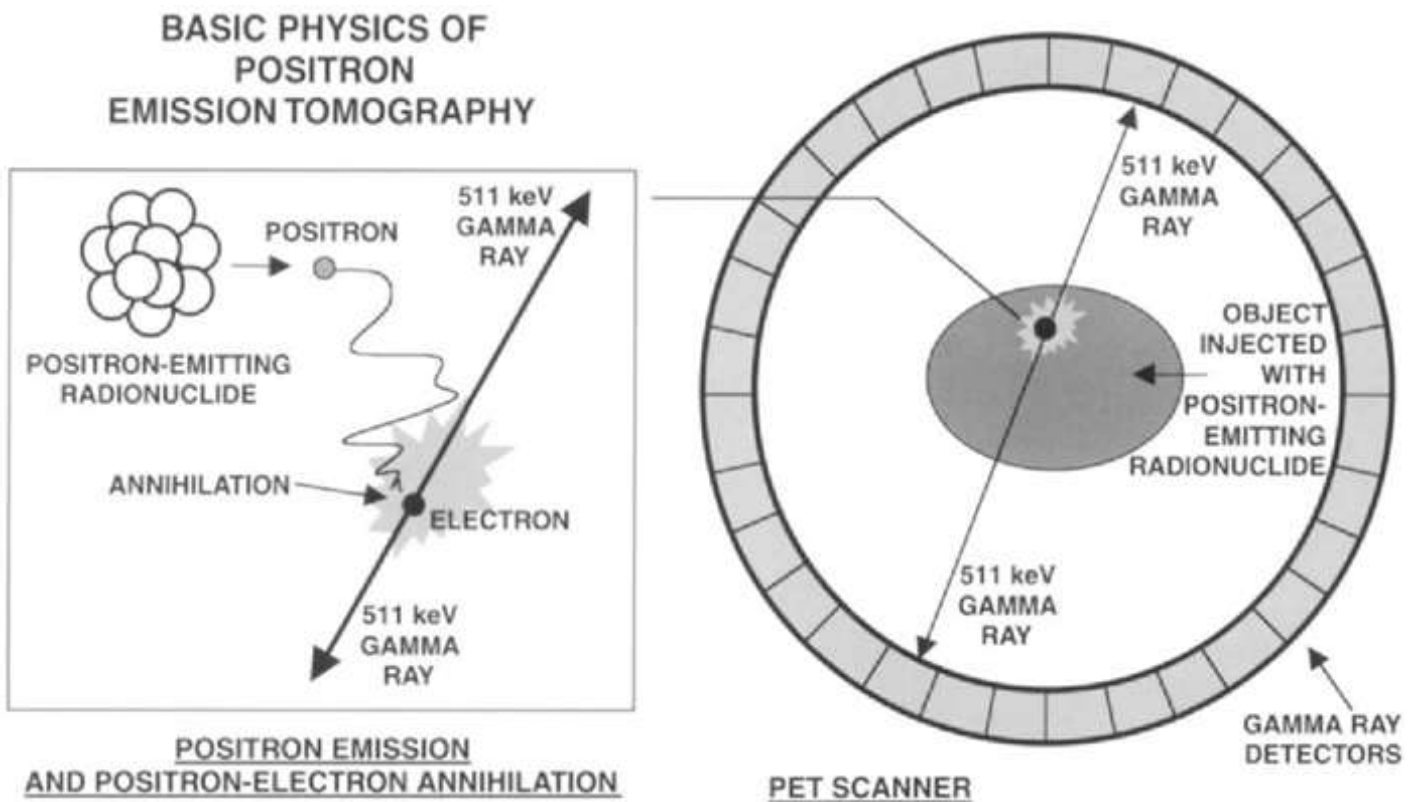
In a cusp trap, particles are confined within the region surrounding the null point, which is achieved by manipulating the strength and direction of the magnetic field. The shape of the magnetic field provides an additional mechanism for confining the particles: as the particles move towards the center of the trap (null point), they encounter the cusp region, where the magnetic field is weakest. At this point, the particles are reflected back towards the walls of the trap, where they experience a stronger magnetic field that prevents them from escaping.

## II. Antimatter use in different fields:

Despite being challenging to produce and store, antimatter has a wide range of potential applications in various fields. This paper will focus on four key areas where antimatter plays a significant role: positron emission tomography (PET), physics research, energy production, and space travel.

### 1. Positron emission tomography (PET) :

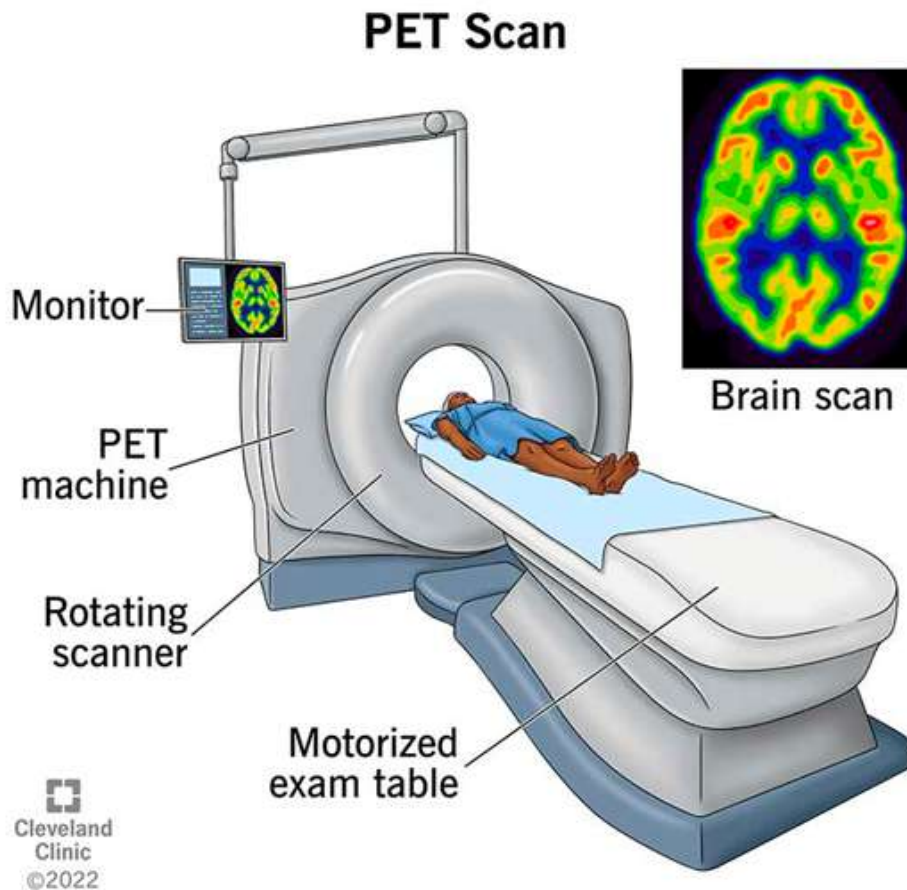
PET works by using a radioactive tracer, which is usually injected into the patient's bloodstream. The tracer emits positrons, which are positively charged particles, as it decays. As shown in figure 9, when a positron meets an electron in the body, they annihilate each other and produce gamma rays, which are detected by a ring of detectors surrounding the body. The detectors capture the gamma rays and use the data to create a 3D image of the body's metabolic and biochemical activity.



**Figure 9: Basic Physics of Positron Emission Tomography**



**Figure 10:** This figure shows a PET machine, which is used to perform PET scans for medical diagnosis and research. The machine consists of a large ring of detectors (not visible in this image) that surrounds the patient. The patient lies still on the scanner bed, which slides in and out of the ring of detectors during the scan.



PET is commonly used to diagnose and monitor a wide range of conditions, including cancer, heart disease, and neurological disorders. It is also used in preclinical research to study the biology of diseases and develop new treatments. PET is a highly sensitive imaging technique that can detect even small changes in metabolism and provide valuable information about disease progression and response to treatment. While PET uses ionizing radiation, the amount of radiation exposure from a typical PET scan is relatively low and considered safe for most patients. PET is a valuable tool in modern medicine, providing physicians and researchers with critical information to help diagnose and treat a wide range of diseases.

## 2. Fundamental physics research: The BASE experiment at CERN

The BASE (Baryon Antibaryon Symmetry Experiment) is a precision physics experiment that takes place at CERN, the European Organization for Nuclear Research. The experiment aims to study the fundamental properties of antimatter, particularly the differences between matter and antimatter.

CPT symmetry, also known as charge-parity-time symmetry, is a fundamental principle in theoretical physics. It states that the laws of physics should remain unchanged when a simultaneous reversal of charge (C), parity (P), and time (T) is applied.

Charge (C) refers to the property of particles being either positively or negatively charged. Parity (P) refers to the spatial orientation or mirror symmetry of a physical system. Time (T) refers to the direction of time, either forward or backward.

The CPT symmetry implies that the behavior of a physical system should be the same regardless of whether particles or antiparticles are involved, whether the spatial coordinates are inverted, or whether time flows forward or backward. Any observed violation of CPT symmetry would have profound implications for our understanding of fundamental physical laws.

The mathematical equations used in the BASE experiment to measure the CPT symmetry of antiprotons involve a combination of classical mechanics and quantum mechanics. Here are the basic steps involved in the experiment:

1. First, the antiprotons are produced in a particle accelerator and then collected in a storage ring.
2. A beam of antiprotons is then extracted from the storage ring and sent through a series of traps and filters to remove unwanted particles.
3. The antiprotons are then captured in a Penning trap, which uses a combination of magnetic and electric fields to confine the particles.
4. The trapped antiprotons are then cooled to very low temperatures using laser cooling techniques, which reduces their thermal motion and improves the precision of the measurements.
5. To measure the mass-to-charge ratio of the antiprotons, the experiment uses the cyclotron frequency method. This involves applying a magnetic field to the trap and then applying a radiofrequency electric field to the antiprotons, causing them to oscillate back and forth in the trap.
6. The frequency of this oscillation is measured using a highly precise detector, and the mass-to-charge ratio of the antiprotons is calculated using the following equation:

$$\frac{m}{q} = \frac{\vec{B}}{\omega}$$

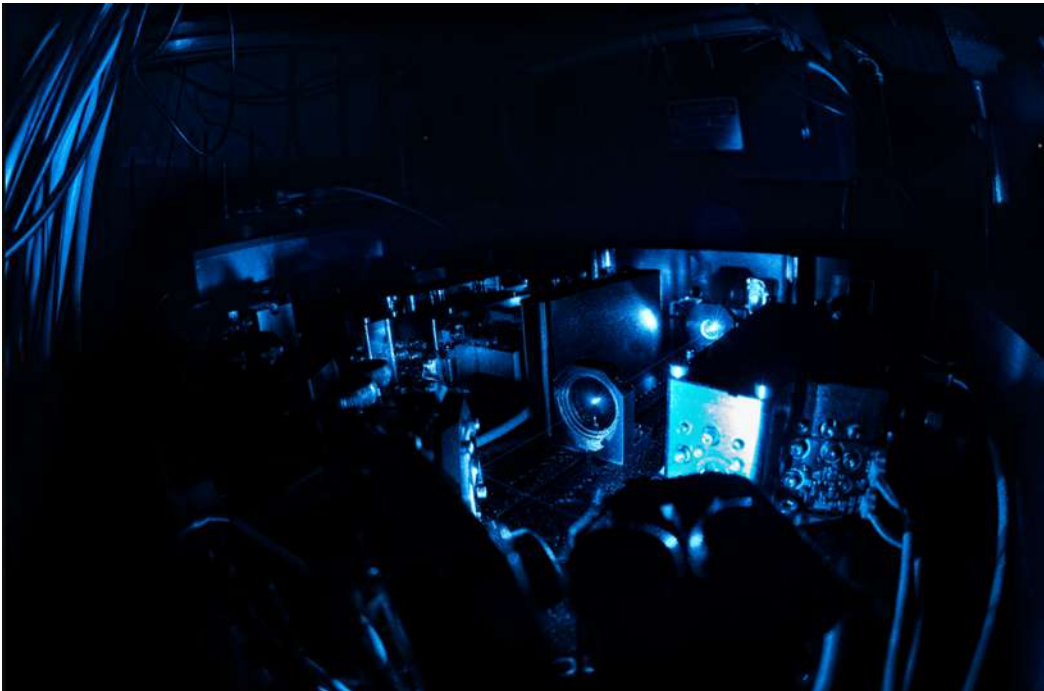
where  $m/q$  is the mass-to-charge ratio of the antiproton,  $q$  is its charge,  $B$  is the magnetic field strength, and  $\omega$  is the frequency of the oscillation.

7. The measured value of the mass-to-charge ratio for the antiprotons is then compared to the corresponding value for protons, which is known with high precision from other experiments.

If the measured value for the antiprotons is consistent with the value for protons, this provides strong evidence for CPT symmetry. If, however, the measured value deviates from the predicted value, this would indicate a violation of CPT symmetry, which would have important implications for our understanding of the fundamental laws of physics

### 3. Fundamental physics research: The ALPHA experiment at CERN

The ALPHA (Antihydrogen Laser Physics Apparatus) experiment is a research project being conducted at the CERN laboratory in Switzerland. Its primary goal is to study the properties of antimatter and test fundamental physics theories. The experiment uses a Penning trap to capture and study antihydrogen atoms, which are made up of an antiproton and a positron. The antihydrogen atoms are created by slowing down antiprotons and positrons and combining them together in a vacuum chamber.

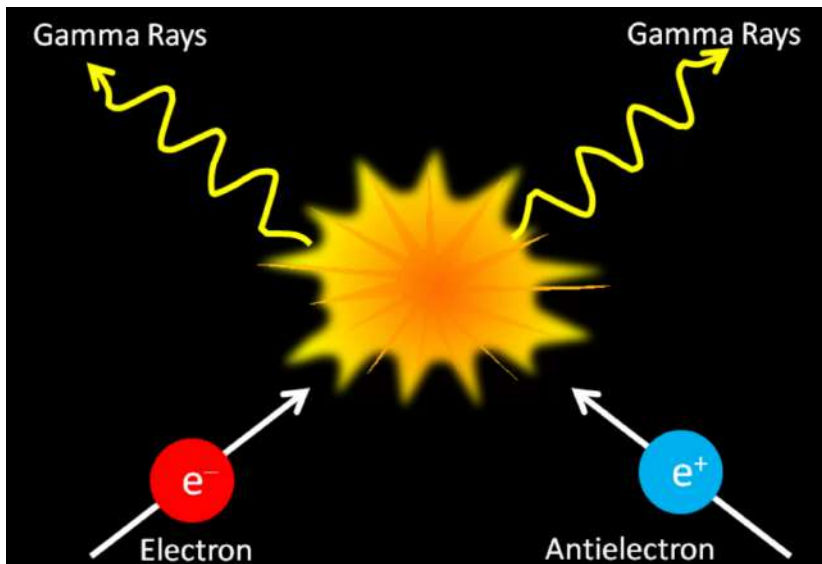


**Figure 11:** The photo shows a setup for laser spectroscopy of antihydrogen as part of the Alpha 2 experiment. In the center of the image, there is a cylindrical vacuum chamber with various optical components surrounding it.

One of the main goals of the ALPHA experiment is to test whether the laws of physics are the same for matter and antimatter. According to the currently accepted theories, matter and antimatter should behave identically, but there may be small differences that have not yet been observed. The experiment has made significant progress in recent years, including the successful production and confinement of antihydrogen atoms for periods of several minutes. This breakthrough has allowed scientists to perform more detailed measurements of the properties of antihydrogen and compare them to those of hydrogen, the simplest and most abundant element in the universe. Overall, the ALPHA experiment is a significant step forward in our understanding of antimatter and fundamental physics. It has the potential to shed light on some of the most fundamental questions about the nature of the universe and the laws that govern it.

### 3- Antimatter as an energy source

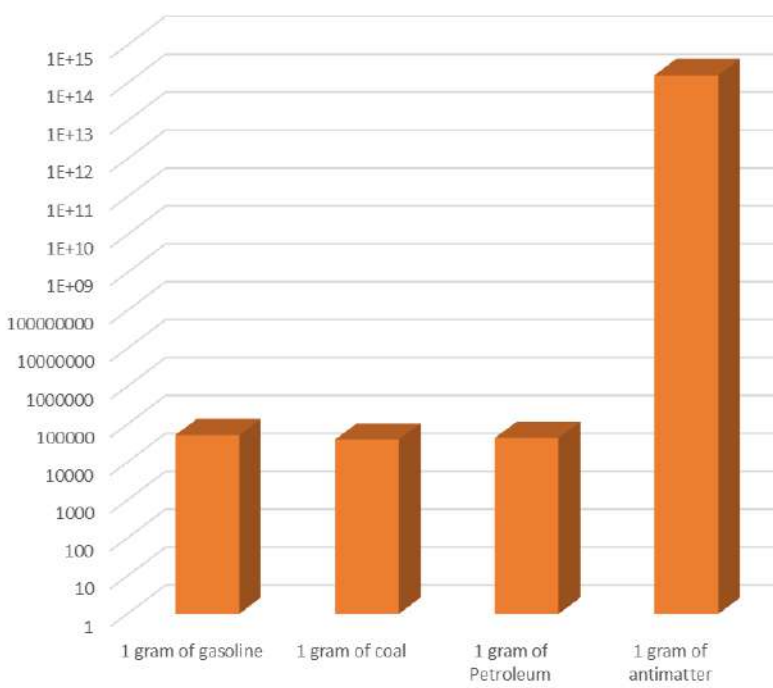
When matter and antimatter particles meet, they annihilate each other and release a significant amount of energy. The annihilation process occurs when a particle (eg. electron fig 12) and its corresponding antiparticle (eg. antielectron fig 12) come into contact and collide. The energy of the collision causes the two particles to annihilate each other, producing energy in the form of gamma rays (yellow arrows fig 12).



**Figure 12:** This figure shows the process of annihilation of an electron and its corresponding antiparticle (called antielectron or positron)

The energy released from the annihilation of a given amount of antimatter and matter is many times greater than the energy released from burning an equivalent amount of fossil fuels.

The **figure 13** compares the amount of energy released per unit mass for different fuels and antimatter. Gasoline, coal, and petroleum release much less energy per unit mass (gram) than antimatter, which has an enormous energy density.



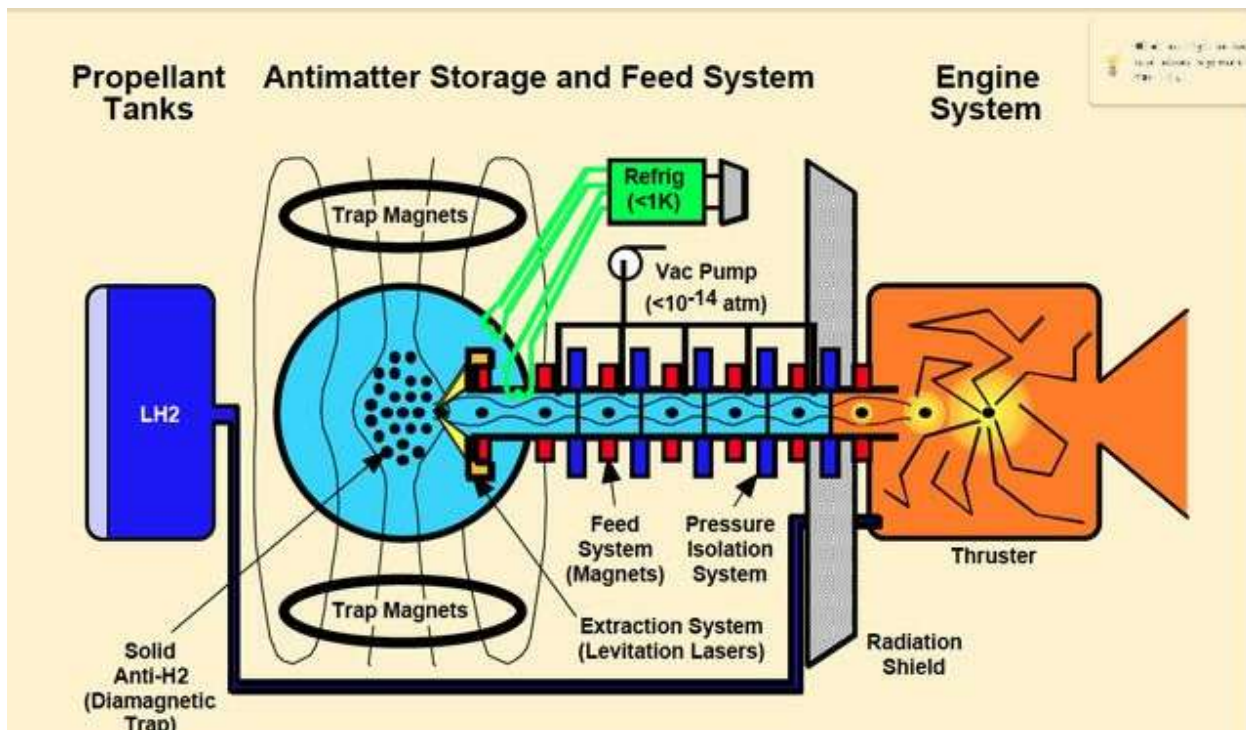
**Figure 13 :** Comparison of energy released per gram for different fuels and antimatter. Antimatter has an enormous energy density, with 1 gram of antimatter releasing more energy than millions of grams of fossil fuels.



#### 4- Antimatter in space travel:

One proposed application of antimatter as an energy source is in space travel. The amount of energy required to accelerate a spacecraft to high speeds is immense, and conventional rocket fuels are limited in their ability to provide the necessary energy. Antimatter, on the other hand, can provide a tremendous amount of energy in a very small package.

The concept behind using antimatter for space travel involves the use of an antimatter-powered engine (fig14). Such an engine would consist of a storage container for the antimatter (a trap), a feed system, and a device to convert the energy released from the annihilation into a useful form of propulsion (engine system fig14). To generate propulsion, the antimatter would be released from its trap and brought into contact with a fuel source, such as hydrogen, which would then undergo a process of annihilation. The energy released would be converted into kinetic energy, propelling the spacecraft forward. The exhaust from this type of engine would consist of a stream of high-energy particles, which would provide thrust to the spacecraft.



**Figure 14:** Diagram of an antimatter-powered engine, showing the main components. The engine uses a propellant tank to store matter, an antimatter storage and feed system to supply antimatter, and an engine system where matter and antimatter meet and annihilate each other, producing energy and thrust.

While the use of antimatter as an energy source for space travel is still in the early stages of research and development, it has the potential to revolutionize space exploration. Antimatter-powered engines could enable spacecraft to travel much faster and more efficiently than conventional rocket engines, potentially allowing us to explore distant parts of our solar system and beyond.



In conclusion, antimatter holds great promise in fields such as positron emission tomography (PET), fundamental physics research, energy production, and space travel. Despite the challenges involved in producing and storing antimatter, its unique properties and immense energy potential make it a valuable resource for advancing scientific knowledge, medical diagnostics, energy technologies, and the future of space exploration.

### III. The matter-antimatter asymmetry problem

The matter-antimatter asymmetry, also known as the baryon asymmetry, is one of the most significant mysteries in modern physics. It refers to the observation that the universe seems to contain much more matter than antimatter, even though both should have been produced in equal amounts during the Big Bang.

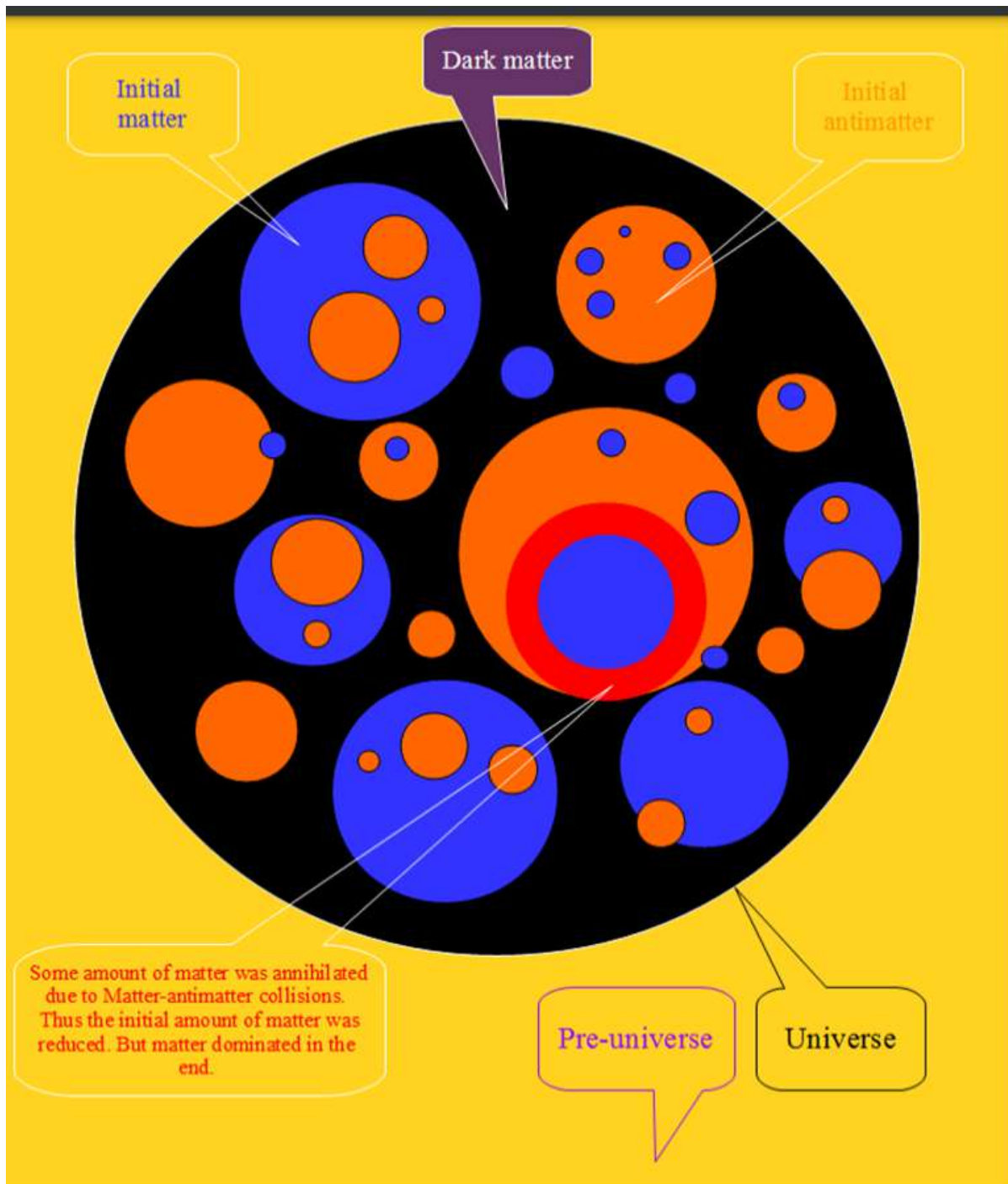
According to the laws of physics, when matter and antimatter come into contact, they annihilate each other, producing high-energy photons. This process should have resulted in the complete annihilation of all matter and antimatter in the universe shortly after the Big Bang, leaving nothing behind.

However, observations show that our universe is filled with matter, and only a tiny amount of antimatter. This observation raises a fundamental question: Why is there more matter than antimatter in the universe?

To explain this asymmetry, physicists have proposed several theories over the years, but none of them have been proven yet. In this paper we will present two of them.

#### ***A. Regions of the universe where antimatter dominate***

The first explanation suggests that matter and antimatter may be separated into different regions of the universe, with antimatter galaxies (orange circles fig 15) existing in widely distant areas. This theory initially proposed that the baryon asymmetry could be explained by the formation of antimatter galaxies, as from a distance, antimatter and matter atoms are indistinguishable, producing light (photons) in the same way. However, the annihilation process and subsequent gamma radiation production along the boundary between matter and antimatter regions would be detectable, depending on distance and density. While no such zones have been detected, it is unlikely that any region within the observable universe is dominated by antimatter, according to research conducted over the last 30 years.



**Figure 15 :** This simplified diagram shows how the imbalance between matter ( blue circles ) and antimatter ( orange circles) could have originated at the beginning of normal time.

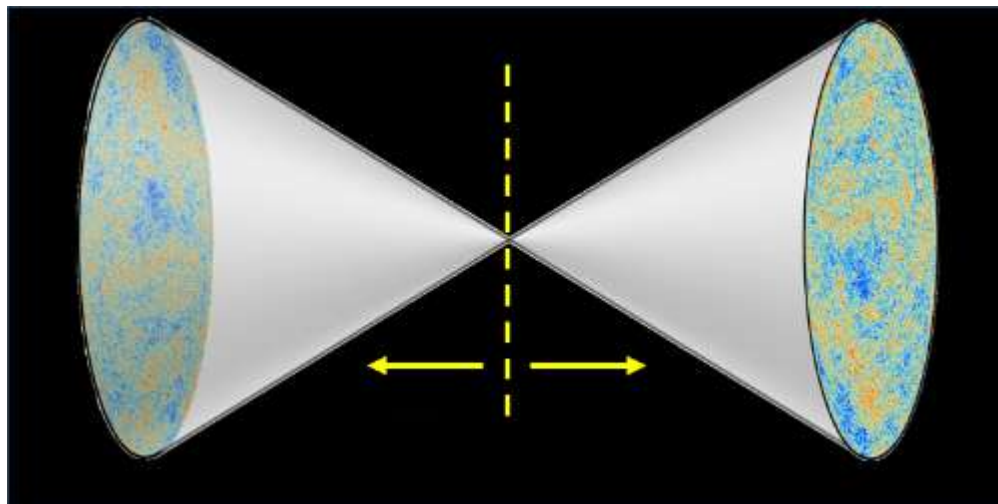
Adapted from : A Possible Solution to the Mystery of the Imbalance Between Matter and Antimatter of the Universe

## B. *The antimatter universe*

The second explanation suggests the existence of a mirror anti-universe. In this scenario, both the universe and its mirror anti-universe emerged from the same Big Bang, but they evolve in opposite directions of time. The mirror universe would be made up mostly of antimatter.

The mirror universe's spatial properties would be inverted relative to ours, meaning that left would be right, and up would be down. The mirror universe's stars and galaxies would appear to rotate clockwise, while the objects in our universe rotate counterclockwise. This inversion of spatial properties arises because particles and their antiparticles have opposite charges, and the mirror universe would be dominated by antimatter.

One of the appealing features of this model is that it gives an explanation of the existence of dark matter. In our universe, dark matter is an invisible substance that seems to make up most of the matter in the universe but does not interact with light. In the mirror universe, the dark matter would be made up of antimatter, which does not interact with light either. This idea has yet to be tested experimentally, but it is an intriguing possibility.



**Figure 16:** The Big Bang generated a universe–antiuniverse pair, our universe flows forward in time, while our mirror counterpart flows backward.



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## **Conclusion:**

In conclusion, the Penning trap, Paul trap, and cusp trap are powerful tools that have been successfully used to confine antimatter. The applications of antimatter are diverse and range from medical imaging to fundamental physics research to space exploration. The BASE and ALPHA experiments at CERN are prime examples of how antimatter can be used to probe the fundamental nature of the universe. Moreover, antimatter has the potential to revolutionize energy production and space travel in the future.

However, the matter-antimatter asymmetry problem remains one of the most profound and challenging questions in physics. The two proposed explanations, the existence of regions in the universe dominated by antimatter and the anti universe theory, require further investigation and experimentation.

Currently, researchers are working tirelessly to explore the properties of antimatter, better understand the matter-antimatter asymmetry problem, and develop new technologies that could harness antimatter's potential. The development of more efficient and precise antimatter traps, such as the proposed ALPHA-g experiment at CERN, could help pave the way for a new era of discovery in antimatter physics.

In the coming years, it is likely that significant progress will be made in this field, leading to a better understanding of the fundamental laws of nature and potentially transformative advancements in various fields. However, much work remains to be done, and the mysteries of antimatter are likely to continue to captivate and challenge scientists for years to come.

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